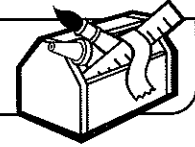


**PROJECT
3****An Ancient Multiplication Method**

Thousands of years ago, the Egyptians developed one of the earliest multiplication methods. Their method uses an idea from number theory.

Every positive whole number can be expressed as a sum of powers of 2.

2^0	2^1	2^2	2^3	2^4	2^5	2^6
1	2	4	8	16	32	64

Write a number sentence to show each of the numbers below as the sum of powers of 2. For example, $13 = 1 + 4 + 8$.

1. $19 =$ _____ 2. $67 =$ _____

Follow the steps below to use the Egyptian method to multiply $19 * 62$.

Step 1 List the powers of 2 that are less than the first factor, 19.

Step 2 List the products of the powers of 2 and the second factor, 62. Notice that each product is double the product before it.

Step 3 Put a check mark next to the powers of 2 whose sum is the first factor, 19.

Step 4 Cross out the remaining rows.

Step 5 Add the partial products that are not crossed out.

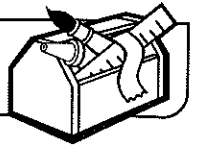
$$62 + 124 + 992 = 1,178$$

$$\text{So } 19 * 62 = 1,178$$

3. Explain why you don't have to multiply by any number other than 2 to write the list of partial products when you use the Egyptian method.

$19 * 62 =$	
1	62
2	124
4	248
8	496
16	992

$19 * 62 = 1,178$	
✓ 1	62
✓ 2	124
4	248
8	496
✓ 16	992

PROJECT
3**An Ancient Multiplication Method *cont.***

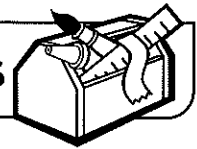
4. Try to solve these problems using the Egyptian method.

$85 * 14 =$ _____	$38 * 43 =$ _____	$45 * 29 =$ _____

Try This

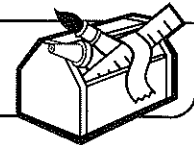
5. Here is another ancient multiplication method, based on the Egyptian method. People living in rural areas of Russia, Ethiopia, and the Near East still use this method. See whether you can figure out how it works. Then try to complete the problem in the third box, using this method.

$13 * 25 =$ <u>325</u>	$38 * 43 =$ <u>1,634</u>	$45 * 29 =$ _____
$\begin{array}{r} 13 \quad 25 \\ \hline 6 \quad 50 \\ 3 \quad 100 \\ 1 \quad 200 \\ \hline 325 \end{array}$	$\begin{array}{r} 38 \quad 43 \\ \hline 19 \quad 86 \\ 9 \quad 172 \\ \hline 4 \quad 344 \\ 2 \quad 688 \\ 1 \quad 1,376 \\ \hline 1,634 \end{array}$	$\begin{array}{r} 45 \quad 29 \\ \hline 22 \quad 58 \\ 11 \quad 116 \\ 5 \quad 232 \\ \hline 2 \quad 464 \\ 1 \quad 928 \\ \hline \end{array}$

PROJECT
3**Comparing Multiplication Algorithms**

Think about the advantages and disadvantages of each multiplication method that you know. Record your thoughts in the chart below.

Algorithm	Advantages	Disadvantages
<p>Partial Products</p> $\begin{array}{r} 43 \\ * 62 \\ \hline 60 [40s] = 2,400 \\ 60 [3s] = 180 \\ 2 [40s] = 80 \\ 2 [3s] = \underline{6} \\ 2,666 \end{array}$		
<p>Lattice</p>		
<p>Egyptian</p> $\begin{array}{r} 43 \quad * \quad 62 \\ \checkmark 1 \quad 62 \\ \checkmark 2 \quad 124 \\ 4 \text{ ————— } 248 \\ \checkmark 8 \quad 496 \\ 16 \text{ ————— } 992 \\ \checkmark 32 \quad \underline{1,984} \\ 2,666 \end{array}$		

**PROJECT
3****Ancient Math Symbols**

1. The ancient Egyptians used picture symbols, called hieroglyphs, to write numbers. Here is how they might have multiplied $11 * 13$ using the algorithm you learned in this project.

= 1	✓ ∩	(1 * 13)
∩ = 10	✓ ∩∩	(2 * 13)
∩ = 100	∩∩∩∩	(4 * 13)
∩ = 1,000	✓	
∩ = 10,000	∩	(8 * 13)
∩ = 100,000	∩ ∩∩∩∩	(11 * 13)
∩ = 1,000,000		

On the back of this sheet, try to multiply $21 * 16$ using the Egyptian algorithm and Egyptian numerals.

2. Do you know any Roman numerals? They were used in Europe for centuries until Hindu-Arabic numerals replaced them. Today, Roman numerals appear mainly in dates on cornerstones and in copyright notices.

It is sometimes said that "multiplication with Roman numerals was impossible." Is that true? See whether you can multiply $12 * 15$ using Roman numerals and the Egyptian algorithm. Use the back of this sheet.

Examples of Roman Numerals:

I = 1 II = 2 III = 3

IV = 4 V = 5 VI = 6

IX = 9 X = 10 XX = 20

XL = 40 L = 50 LX = 60

C = 100 D = 500 M = 1,000